

SAMPLE FROM A 1703 EDITION OF

EUCLID

“THE ELEMENTS”

Euclid was a Greek mathematician, considered the "Father of Geometry". He lived in Alexandria around 300 BC, 2,300 years ago. He is mostly famous for writing this book "THE ELEMENTS" one of the most important books in the history of mathematics. Up to today it is the basis for all geometry school text books.

In the Elements, Euclid deduced the principles of what is now called Euclidean geometry from a small set of axioms. Euclid also wrote works on perspective, conic sections, spherical geometry, number theory and logic.

This edition of the elements in Latin and Greek was printed in Oxford England in the year 1703 under the supervision of David Gregory. David Gregory was an astronomer and university professor. He was a close friend and collaborator of Isaac Newton and helped Newton to publish his famous book the "Principia".

Here I translated the first page which begins with the most basic definition in Geometry, what is a point? "It is something that has no parts". Then I translated proposition 47 which is Euclid's proof of Pythagoras theorem, "the square of the hypotenuse is equal to the sum of the squares of the sides".



The book is leather bound with 700 pages containing all the 13 books of the Elements in two columns, Greek and Latin. The lower picture shows the introduction by Newton's friend David Gregory.



ΕΥΚΛΕΙΔΟΥ
ΤΑ ΣΩΖΟΜΕΝΑ.

E U C L I D I S
QUÆ SUPERSUNT
O M N I A.

EX Recensione DAVIDIS GREGORII M. D.
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O X O N I Æ,
E THEATRO SHELDONIANO, An. Dom. MDCCIII.

ΕΥΚΛΕΙΔΟΥ

ΣΤΟΙΧΕΙΩΝ

BIBLION ΠΡΩΤΟΝ*.

E U C L I D I S

E L E M E N T O R U M

L I B E R P R I M U S.

ΟΡΟΙ.

α'. ΣΗΜΕΙΟΝ ἔστιν, ὃ μέρους ἔστιν.
β'. Γραμμὴ δὲ, μήκος ἀπλατὴς.

γ'. Γραμμῆς δὲ πέρατα, σημεῖα.

δ'. Εὐθεῖα γραμμὴ ἔστιν, ἣ τις ἐξίσω τοῖς ἐφ' ἑαυτῆς σημείοις κείται.

ε'. Επιφάνεια δὲ ἔστιν, ὃ μήκος καὶ πλάτος μόνον ἔχει.

ς'. Επιφανείας δὲ πέρατα, γραμμῆς.

ζ'. Επίπεδος ἐπιφανεία ἔστιν, ἣ τις ἐξίσω ταῖς ἐφ' ἑαυτῆς εὐθείαις κείται.

η'. Επίπεδος δὲ γωνία ἔστιν ἢ ὡς ἐπιπέδω δύο γραμμῶν ἀποκρίναν ἀλλήλων, καὶ μὴ ἐπ' εὐθείας κειμένων, πρὸς ἀλλήλας τῶν γραμμῶν κλίσις.

θ'. Οταν δὲ αἱ περιέχουσαι τὴν γωνίαν γραμμῆς εὐθεῖαι ᾖσιν, εὐθύγραμμος καλεῖται ἡ γωνία.

ι'. Οταν δὲ εὐθεῖα ἐπ' εὐθείας σταθεῖσα ταῖς ἐπὶ τῆς γωνίας ἴσας ἀλλήλας ποιῇ, ὀρθὴ ἔστιν ἑκατέρω τῶν ἴσων γωνιῶν καὶ ἡ ἐπὶ τῆς εὐθείας καθετοῦ καλεῖται ἐφ' αὐτῆς ἐρέσθαι.

ια'. Ἀμβλεία γωνία ἔστιν, ἢ μείζων ὀρθῆς.

ιβ'. Ὄξεια δὲ, ἢ ἐλάσσων ὀρθῆς.

ιγ'. Οεὸς ἔστιν, ὃ πρὸς ἑστὶ πέρατα.

DEFINITIONES.

1. PUNCTUM est, cuius pars nulla est.
2. Linea autem est longitudo non lata.

3. Lineæ vero extrema sunt puncta.

4. Recta quidem linea est, quæ ex æquo sua interjacet puncta.

5. Superficies autem est, quod longitudinem & latitudinem tantum habet.

6. Superficiei vero extrema sunt lineæ.

7. Plana quidem superficies est, quæ ex æquo suas lineas rectas interjacet.

8. Planus vero angulus est duarum linearum, in plano scilicet tangentium, & non in directum jacentium, mutua inclinatione.

9. Quando autem lineæ angulum comprehendentes rectæ fuerint, angulus ipse appellatur rectilineus.

10. Cum vero recta linea super rectam lineam insitens angulos deinceps inter se æquales fecerit, rectus est uterque æqualium angulorum: & quæ insitit recta linea, perpendicularis vocatur ad eam super quam insitit.

11. Obtusus angulus est, qui major est recto.

12. Acutus autem, qui est recto minor.

13. Terminus est, quod alicujus est extremum.

* Quidam Codices addunt: καὶ τῶν ὀρθῶν ἐπιπέδων



*Aristippus Philosophus Socraticus, naufragio cum ejectus ad Rhodiensium
litus animadvertisset Geometrica schemata descripta, exclamavisse ad
comites ita dicitur, Bene speremus, Hominum enim vestigia video.
Vitruv. Architect. lib. 6. Præf.*

PROP. XLVII. THEOR.

In rectangulis triangulis, quadratum, quod à latere rectum angulum subtendente describitur, æquale est quadratis, quæ à lateribus rectum angulum comprehendentibus describuntur.

SIT triangulum rectangulum ABΓ, rectum habens ΒΑΓ angulum: dico quadratum, descriptum à recta ΒΓ, æquale esse quadratis, quæ ab ipsis ΒΑ, ΑΓ describuntur.

Describatur enim à ΒΓ quidem quadratum ΒΔΕΓ; ab ipsis vero ΒΑ, ΑΓ quadrata ΗΒ, ΘΓ; perque Α alterutri ipsarum ΒΔ, ΓΕ parallela ducatur ΑΑ; & ducantur ΑΔ, ΖΓ.

Quoniam igitur uterque angulorum ΒΑΓ, ΒΑΗ rectus est; & ad eandem rectam lineam ΒΑ, & ad punctum in ea Α, dux rectæ lineæ ΑΓ, ΑΗ, non ad easdem partes posite, faciunt angulos deinceps duobus rectis æquales: ΓΑ recta est in directum ipsi ΑΗ. eadem ratione, & ΑΒ est in directum ipsi ΑΘ. & quoniam angulus ΔΒΓ [per 10. ax.] est æqualis angulo ΖΒΑ, rectus enim est uterque, communis addatur ΑΒΓ: totus igitur ΔΒΑ angulus toti ΖΒΓ est æqualis. cum autem dux ΔΒ, ΒΑ duabus ΓΒ, ΒΖ sint æquales, altera alteri, & angulus ΔΒΑ æqualis angulo ΖΒΓ: erit [per 4. prop.] & basis ΑΔ basi ΖΓ æqualis, & ΑΒΔ triangulum triangulo ΖΒΓ æquale. estque trianguli quidem ΑΒΔ [per 41. prop.] duplum ΒΑ parallelogrammum; basim enim eandem habent ΒΔ, & sunt in eisdem parallelis ΒΔ, ΑΑ: trianguli vero ΖΒΓ duplum est ΗΒ quadratum; rursus enim basim habent eandem ΖΒ, & sunt in eisdem parallelis ΖΒ, ΗΓ; æqualium autem dupla sunt inter se æqualia: æquale est igitur parallelogrammum ΒΑ ipsi ΗΒ quadrato. similiter, ductis ΑΕ, ΒΚ, ostendetur etiam ΓΑ parallelogrammum æquale quadrato ΘΓ: totum igitur ΒΔΕΓ quadratum duobus quadratis ΗΒ, ΘΓ est æquale. & est quidem ΒΔΕΓ quadratum à recta linea ΒΓ descriptum; quadrata vero ΗΒ, ΘΓ ab ipsis ΒΑ, ΑΓ: quadratum igitur ΒΕ, à latere ΒΓ descriptum, æquale est quadratis, quæ describuntur à lateribus ΒΑ, ΑΓ.

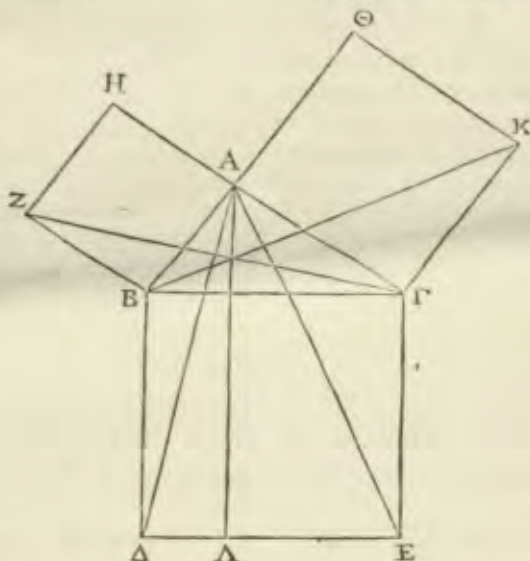
Ergo in rectangulis triangulis, quadratum, quod à latere rectum angulum subtendente describitur, æquale est quadratis, quæ à lateribus rectum angulum comprehendentibus describuntur. quod erat demonstrandum.

ΠΡΟΤΑΣΙΣ μζ.

Εν τοῖς ὀρθογώνιοις τριγώνοις, τὸ ἀπὸ τῆς ὀρθῆς γωνίας ὑποτείνουσης πλευρᾶς πε- τεράγωνοι ἴσον ἐστὶ τοῖς ἀπὸ τῆς ὀρθῆς γωνίας ὀρθογώνιοις πλευρῶν, τετραγώνοις.

ΕΣΤΩ τριγώνον ὀρθογώνιον τὸ ΑΒΓ, ὀρθῆς ἔχον πλάτος ὑπὸ ΒΑΓ· λέγω ὅτι τὸ ἀπὸ τῆς ΒΓ πε- τεράγωνοι ἴσον ἐστὶ τοῖς ἀπὸ τῆς ΒΑ, ΑΓ πετραγώνοις.

Αναγεγράφθω γὰρ ἀπὸ τοῦ Α ἡ ΒΓ παράλληλος τῆς ΒΑ, ΑΓ τὰς ΗΒ, ΘΓ· καὶ διὰ τῆς Α ὀπίσσω τῶν ΒΔ, ΓΕ παράλληλος ἡ ΧΔ ἢ ΑΔ· καὶ ἐπιζεύχθωσαν αἱ ΑΔ, ΖΓ.



Καὶ ἐπεὶ ὀρθὴ ἐστὶν ἑκα- τέρῃ τῶν ὑπὸ ΒΑΓ, ΒΑΗ γωνιῶν· ὡς δὴ πρὶ τῆς ΒΑ, καὶ τῶν πρὸς αὐτῇ ση- μείῳ τῶν Α, δύο εὐθείαι αἱ ΑΓ, ΑΗ, μὴ ὄντι τὰ αὐτὰ μέρη κείδημαι, πρὸς ἐφεξῆς γωνίας δυσὶν ὀ- ρθῶν ἴσους ποιῶσιν· ἐπ' εὐθείας ἄρα ἐστὶν ἡ ΓΑ τῇ ΑΗ, δια τὰ αὐτὰ δὴ καὶ ἡ ΑΒ τῇ ΑΘ ἐστὶν ἐπ' εὐ- θείας. καὶ ἐπει ἴση ἐστὶν ἡ ὑπὸ ΔΒΓ γωνία τῇ ὑπὸ ΖΒΑ, ὀρθὴ γὰρ ἑκατέρα, κοινὴ προσκείδηται ἡ ὑπὸ ΑΒΓ· ὅλη ἄρα ἡ ὑπὸ ΔΒΑ ὅλη τῇ ὑπὸ ΖΒΓ ἐστὶν ἴση. Ἐ- πεί δὲ δύο αἱ ΔΒ, ΒΑ δυ-

οῖ τῶν ΓΒ, ΒΖ ἴση ἐστὶν, ἑκατέρα ἑκατέρα, καὶ γωνία ἡ ὑπὸ ΔΒΑ γωνία τῇ ὑπὸ ΖΒΓ ἴση ἐστὶν· βά- σις ἄρα ἡ ΑΔ βάσι τῇ ΖΓ ἐστὶν ἴση, καὶ τὸ ΑΒΔ τριγώνον τῷ ΖΒΓ τριγώνῳ ἐστὶν ἴσον. καὶ ἐστὶ δὲ μὲν ΑΒΔ τριγώνον διπλάσιον τὸ ΒΑ ὀρθογώνιον, βάσιν τε γὰρ τῷ αὐτῷ ἔχει τὴν ΒΔ καὶ ἐπ' αὐτῆς εἰσι ὀρθογώνιοι τῶν ΒΔ, ΑΑ· ὅ ἢ ΖΒΓ τριγώνον διπλάσιον τὸ ΗΒ τετραγώνον, βάσιν τε γὰρ πάλιν τῷ αὐτῷ ἔχει τὴν ΖΒ καὶ ἐπ' αὐτῆς ὀρθογώνιοι εἰσι τῶν ΖΒ, ΗΓ· τὰ δὲ τῶν ἴσων δι- πλάσια ἴσα ἀλλήλοις ἐστὶν· ἴσον ἄρα ἐστὶ καὶ τὸ ΒΑ ὀρθογώνιον τῷ ΗΒ τετραγώνῳ. ὁμοίως δὲ, ὄντι ὀρθογώνιοι τῶν ΑΕ, ΒΚ, διακείδηται καὶ τὸ ΓΑ ὀρθογώνιον ἴσον τῷ ΘΓ τετραγώνῳ· ὅλον ἄρα τὸ ΔΒΓΕ τετραγώνον δυσὶ τοῖς ΗΒ, ΘΓ τετραγώνοις ἴσον ἐστὶ. καὶ ἐστὶ τὸ μὲν ΒΔΕΓ τετραγώνον ἀπὸ τῆς ΒΓ ἀναγεφέν, τὰ δὲ ΗΒ, ΘΓ ἀπὸ τῆς ΒΑ, ΑΓ· τὸ ἄρα ἀπὸ τῆς ΒΓ πλευρᾶς τετραγώνον ΒΕ ἴσον ἐστὶ τοῖς ἀπὸ τῆς ΒΑ, ΑΓ πλευρῶν τετραγώνοις.

Εν ἄρα τοῖς ὀρθογώνιοις τριγώνοις, τὸ ἀπὸ τῆς ὀρθῆς γωνίας ὑποτείνουσης πλευρᾶς πε- τεράγωνοι ἴσον ἐστὶ τοῖς ἀπὸ τῆς ὀρθῆς γωνίας ὀρθογώνιοις πλευρῶν, τετραγώνοις. ὅπερ εἶδει δεῖξαι.

TRANSLATIONS

Shipwreck caption

When Aristippus the Socratic philosopher, casted by a shipwreck at the coast of Rhodesia, noticed a geometry drawing on the sand, he said: "Now we have good hope because I see traces of men".

First Book

Definitions

1. A point is something without parts.
2. A line is length but not width.
3. The ends of a line are points.
4. A straight line is made of evenly laid points.
5. A surface is something that has length and width.
6. The ends of a surface are lines.
7. A flat surface is made of evenly laid straight lines.
8. A plane angle is made of two lines that touch, are inclined to each other and are not in a straight line.
9. When the lines that make the angle are straight the angle is called rectilinear.
10. When a straight line on another straight line makes adjacent angles equal to one another, each of the equal angles is right and the straight line is called perpendicular to the one on which lays.
11. An obtuse angle is greater than a right angle.
12. An acute angle is smaller than a right angle.
13. A boundary is the extreme of anything.

Proposition 47 (Pythagorean theorem)

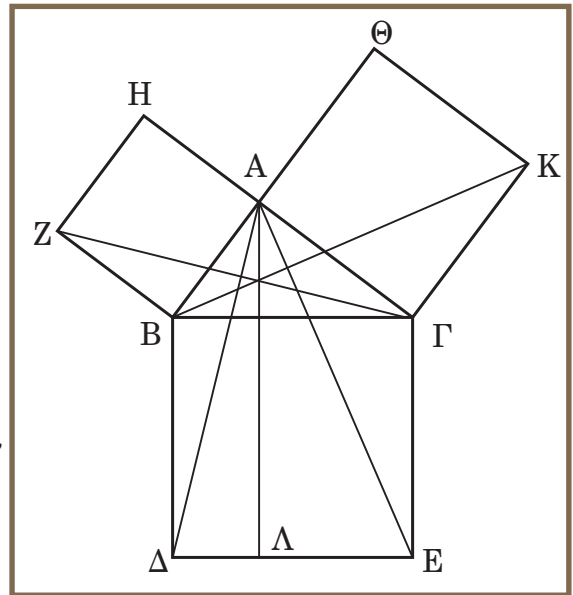
In right angled triangles the square on the side described as subtending the right angle is equal to the squares of the sides making the right angle.

Let $AB\Gamma$ be a right angled triangle having the right angle $B\Lambda\Gamma$. I say that the square on $B\Gamma$ is equal to the squares on BA and $A\Gamma$.

Let there be the square $B\Delta E\Gamma$ described on $B\Gamma$ the square $B\Delta E\Gamma$, and on $BA, A\Gamma$ the squares $HB, \Theta\Gamma$; through A let $\Lambda\Lambda$ be drawn parallel to either $B\Delta$ or ΓE , and let $A\Delta, Z\Gamma$ be joined.

Because each of the angles $B\Lambda\Gamma, B\Lambda H$ is right, it follows that with a straight line BA and a point A on it, the two straight lines $A\Gamma, AH$ not laying on the same side make the adjacent angles to two right angles; therefore ΓA is in a straight line with AH .

For the same reason BA is also in straight line with $A\Theta$. And, since the angle $\Delta B\Gamma$ is equal to the angle ZBA , because each is right, let the angle $AB\Gamma$ be added to each; therefore the whole angle ΔBA is equal to the whole angle $ZB\Gamma$.



And, since ΔB is equal to $B\Gamma$, and ZB to BA , the two sides $AB, B\Delta$ are equal to the two sides $ZB, B\Gamma$ respectively, and the angle $AB\Delta$ is equal to the angle $ZB\Gamma$; therefore the base $A\Delta$ is equal to the base $Z\Gamma$, and the triangle $AB\Delta$ is equal to the triangle $ZB\Gamma$.

Now the parallelogram $B\Lambda$ is double of the triangle $AB\Delta$, for they have the same base $B\Delta$ and are in the same parallels $B\Delta, \Lambda\Lambda$. And the square HB is double of the triangle $ZB\Gamma$, because they have again the same base ZB , and are the same parallels $ZB, H\Gamma$. But the doubles of equals are equal to one another.

Therefore the parallelogram $B\Lambda$ is also equal to the square HB ; Similarly. If $A\Gamma$ is joined to BK , the parallelogram $\Gamma\Lambda$ can also be proved equal to the square $\Theta\Gamma$; therefore the whole square $B\Delta E\Gamma$ is equal to the two squares $HB, \Theta\Gamma$. And the square $B\Delta E\Gamma$ is described on $B\Gamma$, and the squares $HB, \Theta\Gamma$ on $BA, A\Gamma$.

Therefore the square on the side $B\Gamma$ is equal to the squares on the sides $BA, A\Gamma$.

Therefore in a right triangle the square on the side described as subtending the right angle is equal to the squares of the sides making the right angle. Which is what was to be demonstrated.

The Greek Language

The Greek language holds an important place in the histories of Europe, the more loosely defined "Western" world, and Christianity; the canon of ancient Greek literature includes works of monumental importance and influence for the future Western canon, such as the epic poems Iliad and Odyssey.

Greek was also the language in which many of the foundational texts of Western philosophy, such as the Platonic dialogues and the works of Aristotle, were composed; The New Testament of the Christian Bible was written in Koiné Greek and the liturgy continues to be celebrated in the language in various Christian denominations (particularly the Eastern Orthodox and the Greek Rite of the Catholic Church).

Together with the Latin texts and traditions of the Roman world (which was profoundly influenced by ancient Greek society), the study of the Greek texts and society of antiquity constitutes the discipline of Classics.

Greek was a widely spoken lingua franca in the Mediterranean world and beyond during Classical Antiquity, and would eventually become the official parlance of the Byzantine Empire. In its modern form, it is the official language of Greece and Cyprus and one of the 23 official languages of the European Union. The language is spoken by approximately 13 million people today in Greece, Cyprus, and diaspora communities in numerous parts of the world.

The Greek Alphabet

Αα	Alpha	Νν	Nu
Ββ	Beta	Ξξ	Xi
Γγ	Gamma	Οο	Omicron
Δδ	Delta	Ππ	Pi
Εε	Epsilon	Ρρ	Rho
Ζζ	Zeta	Σσς	Sigma
Ηη	Eta	Ττ	Tau
Θθ	Theta	Υυ	Upsilon
Ιι	Iota	Φφ	Phi
Κκ	Kappa	Χχ	Chi
Λλ	Lambda	Ψψ	Psi
Μμ	Mu	Ωω	Omega

I encourage you to learn and master another language. It will expand your understanding of other cultures and ways of thinking. Greek roots are often used to coin new words for other languages, especially in the sciences and medicine; Greek and Latin are the predominant sources of the international scientific vocabulary. Over fifty thousand English words are derived from the Greek language.